

# Grid Computing

## introduction & illustration

T. Gautier  
V. Danjean

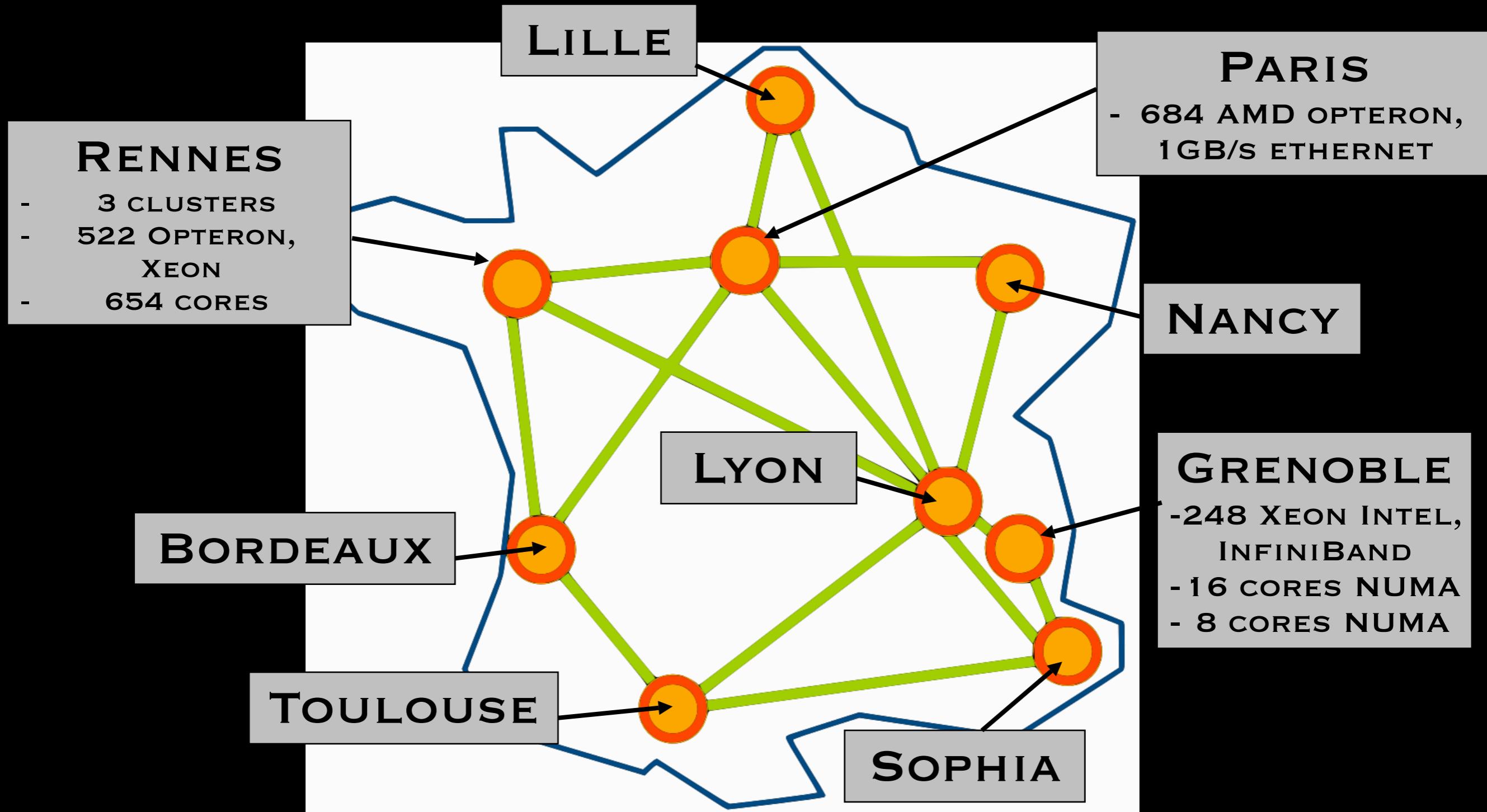
# Facts

- No choice : parallelism is in any computer
    - MPSoC, Multicore, Manycore, Cluster, Grid
  - Exact Solution to the Quadratic Assignment Problem
    - Combinatorial Problem: NUG30, 7 days, 650 processors
  - Solving bigger CFD, CEM problems
    - 100GBytes of memory
- ➡ Cluster & Grid computing

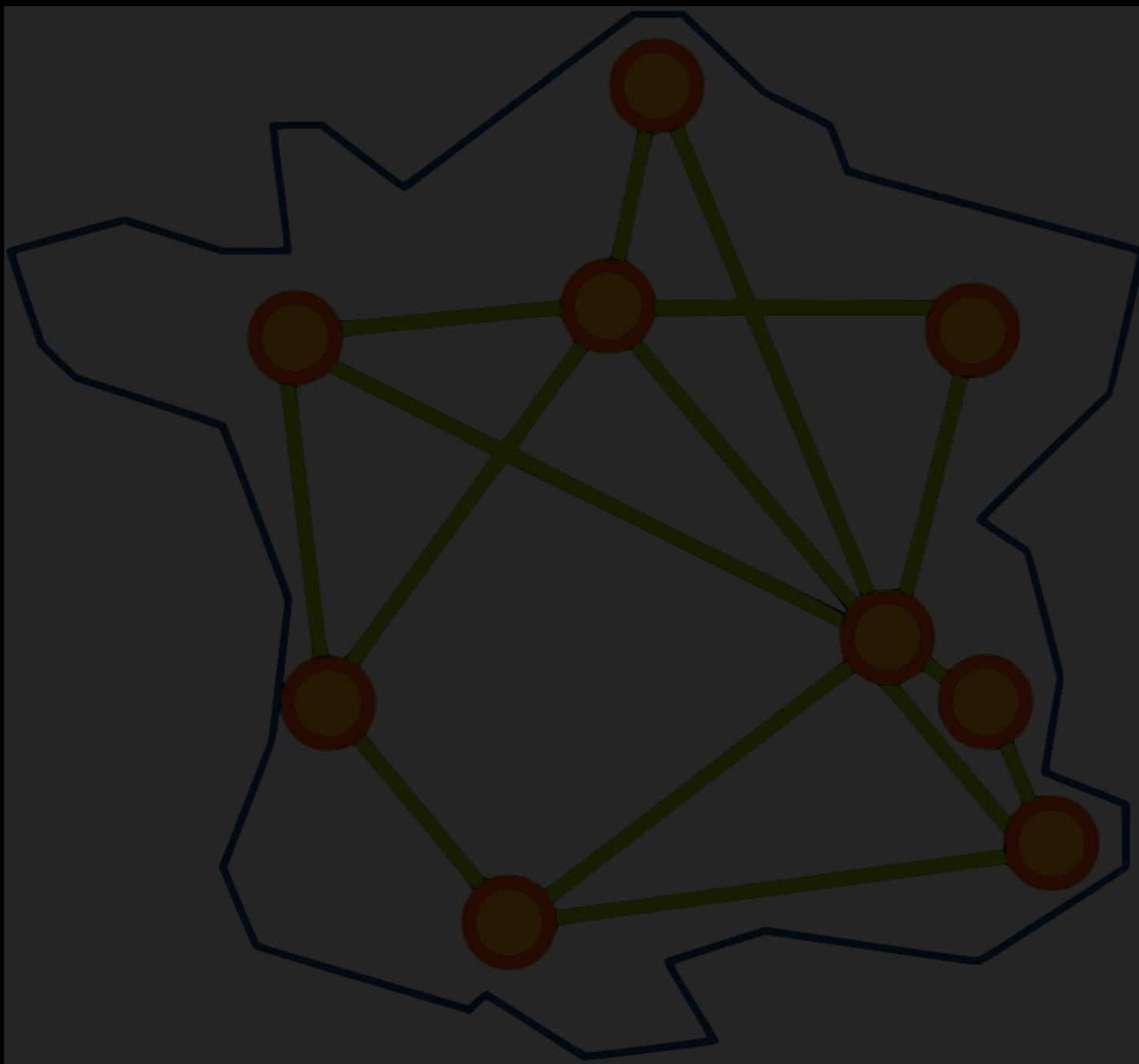
# Outline

- Context
  - Parallel and distributed architecture
- Programming Challenges
  - Parallel algorithm
  - Scheduling & Communication
- Illustration with domain decomposition method
- Conclusions

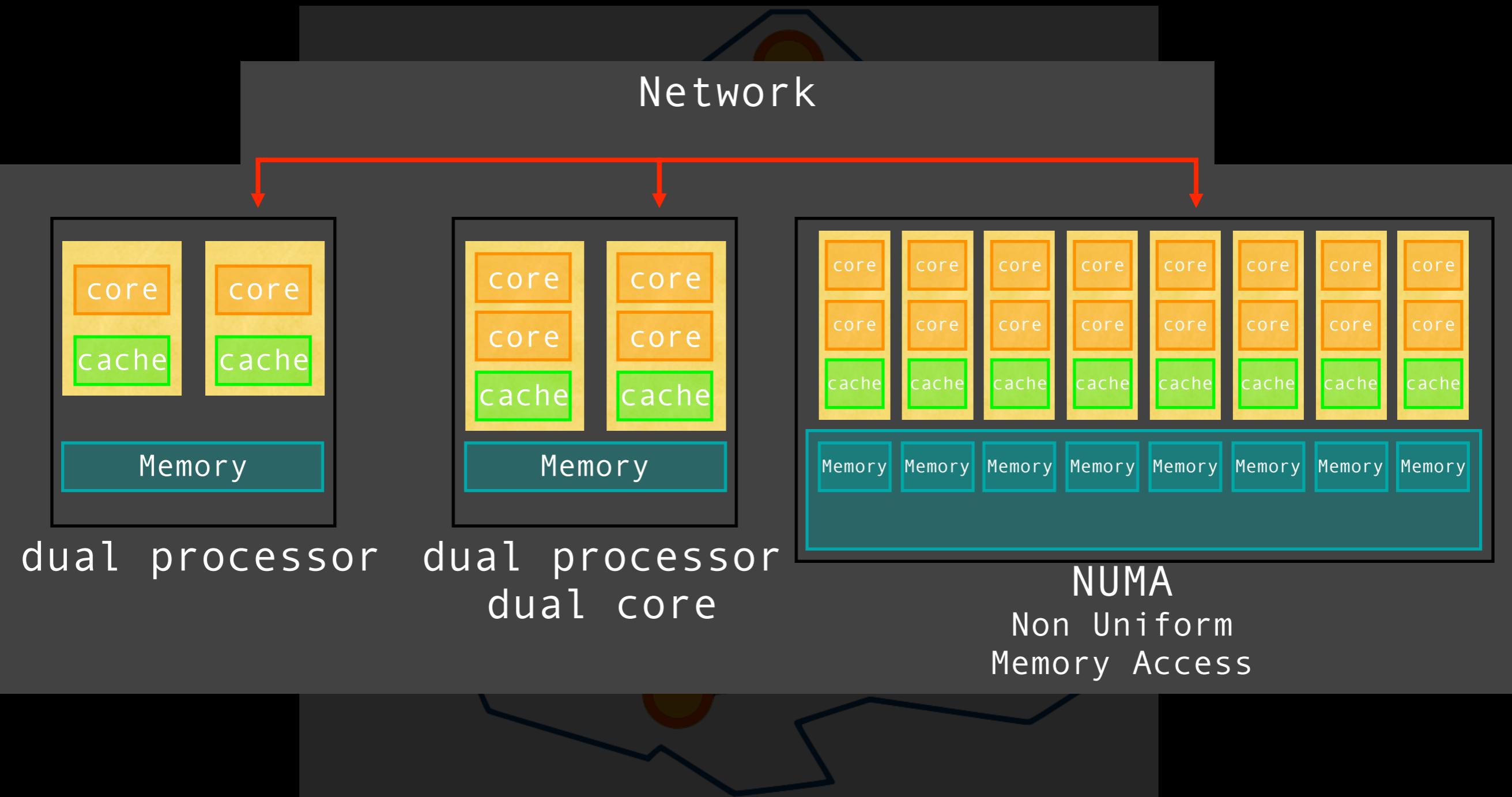
# [www.grid5000.fr](http://www.grid5000.fr)



# Grid5000



# Grid5000



# Characteristics

- Cluster: set of homogeneous machines
  - homogeneous resources (memory, cpu)
    - Dual, Quad, Octo cores cpu, GBytes / machine
  - homogeneous & high performance network
    - Ethernet, Myrinet, InfiniBand
  - homogeneous administration domain
    - 1 user = 1 account, home directory mounted using NFS

# Characteristics

- Grid: set of clusters
  - heterogeneous resources
    - CPU, memory, network speed
    - Each cluster has different number of machines
  - Network between clusters: high latency !
  - multiple administration domains
    - 1 user = multiple account
    - access to cluster through firewall
  - dependability problem
    - huge number of basic components

# Programming Challenges

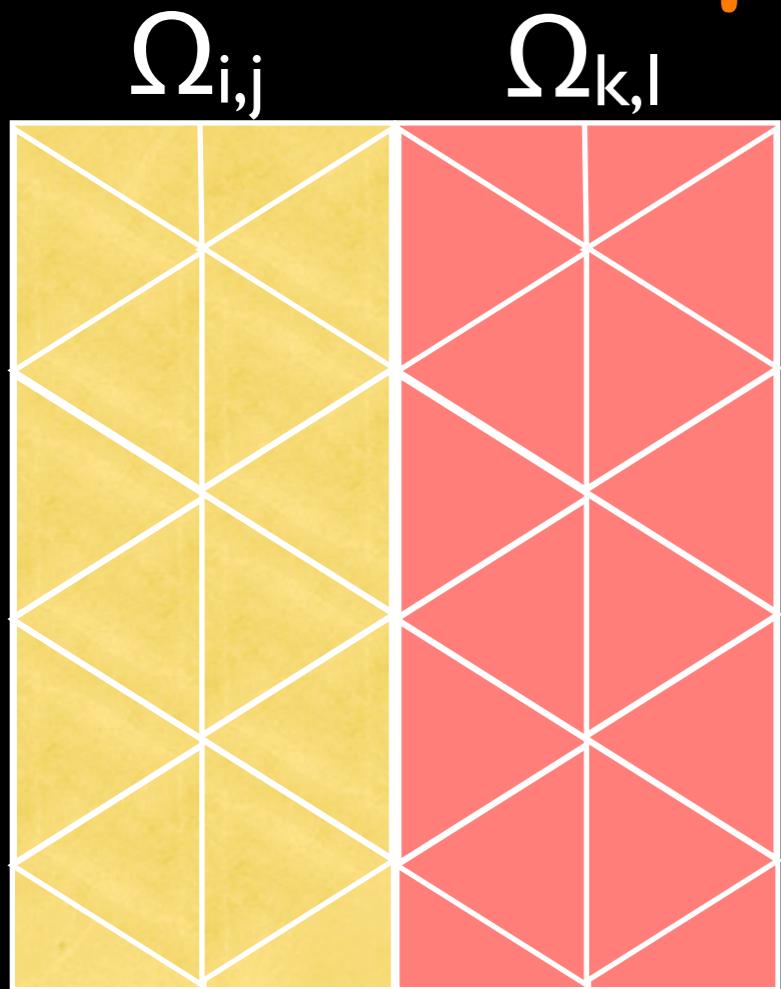
- Write once, run anywhere
  - heterogeneity !
- Keypoints
  - parallel algorithm
  - scheduling
  - implementation
  - [fault tolerance]

# Parallel algorithm

- 30 years of theoretical studies & experiments of parallel architectures
- What's new ?
  - huge number of cores/CPU
  - fault tolerance
    - ABFT: Algorithm Based Fault Tolerant

# Let's back to a problem

- Domain decomposition for matrix vector product



$$(Ax)_{i,j} = \begin{pmatrix} B_{i,j} & E_{i,j} \\ F_{i,j} & C_{i,j} \end{pmatrix} \begin{pmatrix} u_{i,j} \\ v_{i,j} \end{pmatrix} + \left( \sum_{\Omega_{k,l} \in N_{i,j}} E_{i,j}^{k,l} v_{k,l} \right)$$

# Let's back to a problem

- Domain decomposition for matrix vector product

The diagram illustrates domain decomposition. On the left, a large square domain is divided into two sub-domains:  $\Omega_{i,j}$  (yellow) and  $\Omega_{k,l}$  (red). A green arrow points from this decomposition to a mathematical equation on the right.

$$(Ax)_{i,j} = \begin{pmatrix} B_{i,j} & E_{i,j} \\ F_{i,j} & C_{i,j} \end{pmatrix} \begin{pmatrix} u_{i,j} \\ v_{i,j} \end{pmatrix} + \left( \sum_{\Omega_{k,l} \in N_{i,j}} E_{i,j}^{k,l} v_{k,l} \right)$$

Annotations below the equation identify components: "local internal values" points to the  $(B_{i,j}, E_{i,j})$  block, and "local interface values" points to the  $E_{i,j}^{k,l}$  term.

# Let's back to a problem

- Domain decomposition for matrix vector product

The diagram illustrates domain decomposition. On the left, a large square domain is divided into two overlapping subdomains,  $\Omega_{i,j}$  (yellow) and  $\Omega_{k,l}$  (red). A green arrow points from this decomposition to a mathematical equation on the right.

The equation represents the computation of a matrix-vector product  $(Ax)_{i,j}$  for a subdomain  $\Omega_{i,j}$ . It is decomposed into three components:

$$(Ax)_{i,j} = \begin{pmatrix} B_{i,j} & E_{i,j} \\ F_{i,j} & C_{i,j} \end{pmatrix} \begin{pmatrix} u_{i,j} \\ v_{i,j} \end{pmatrix} + \left( \sum_{\Omega_{k,l} \in N_{i,j}} E_{i,j}^{k,l} v_{k,l} \right)$$

Annotations explain the terms:

- local internal values:** Points to the  $B_{i,j}$  and  $C_{i,j}$  blocks of the matrix.
- local interface values:** Points to the  $E_{i,j}$  block of the matrix.
- external interface values:** Points to the summation term involving  $E_{i,j}^{k,l}$ .

# Scheduling

- Once tasks and data are described by a parallel algorithm then:
  - For each task, compute where to execute it
  - For each data, compute where to store it
- Such that:
  - Completion time is minimize, ...
- NP-hard problem
  - Use algorithms to approximate the problem
  - Use heuristics, application dependent

# Strict multi-threaded computations

## ● Notations

- $T_s$  : Sequential work, time of sequential execution
- $D$  : Critical Path
- $P$ : the  $P$  processors

## ● Properties

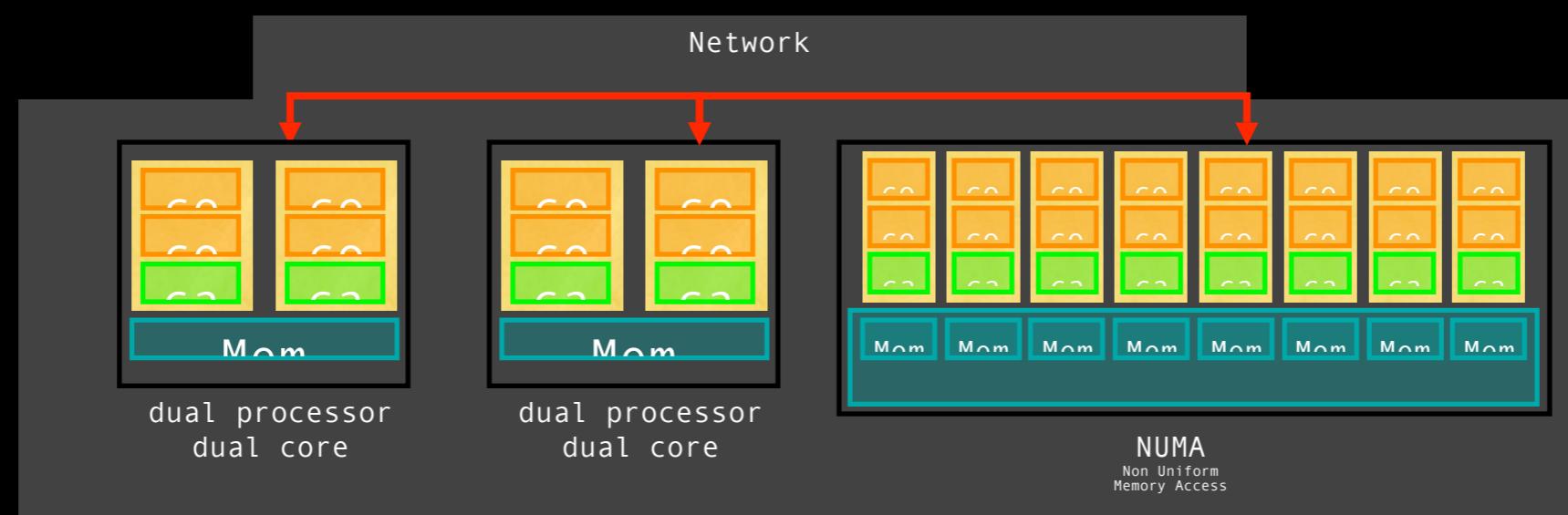
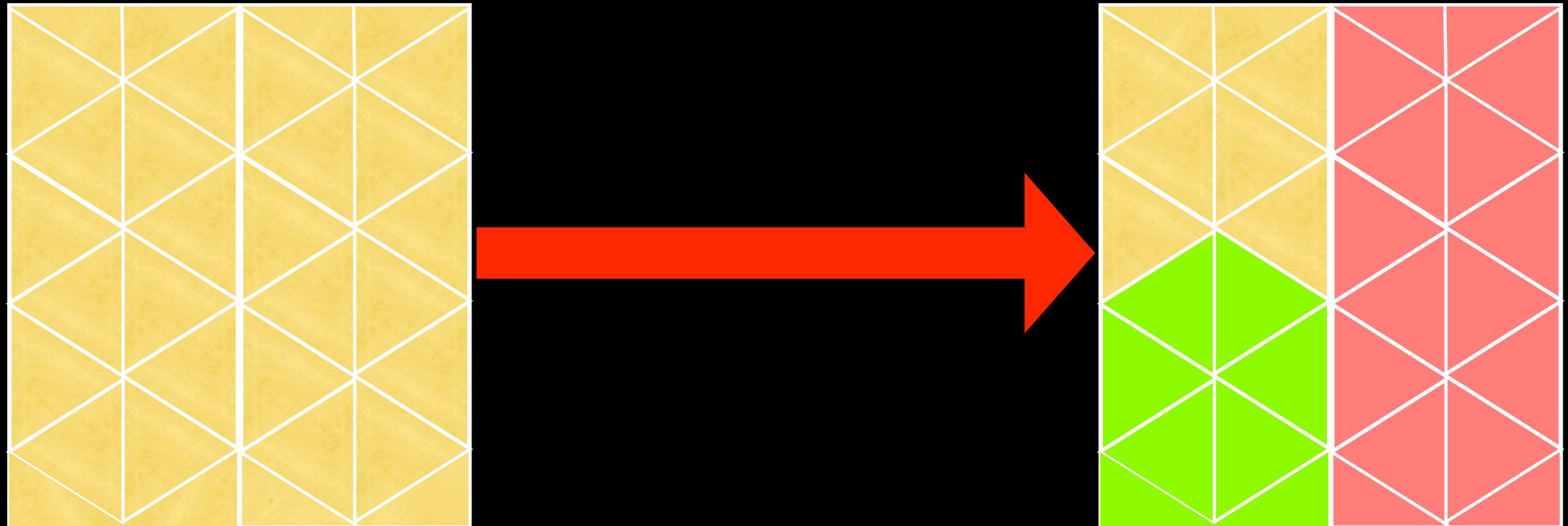
- with high probability, number of steals is

$$O(P \times D)$$

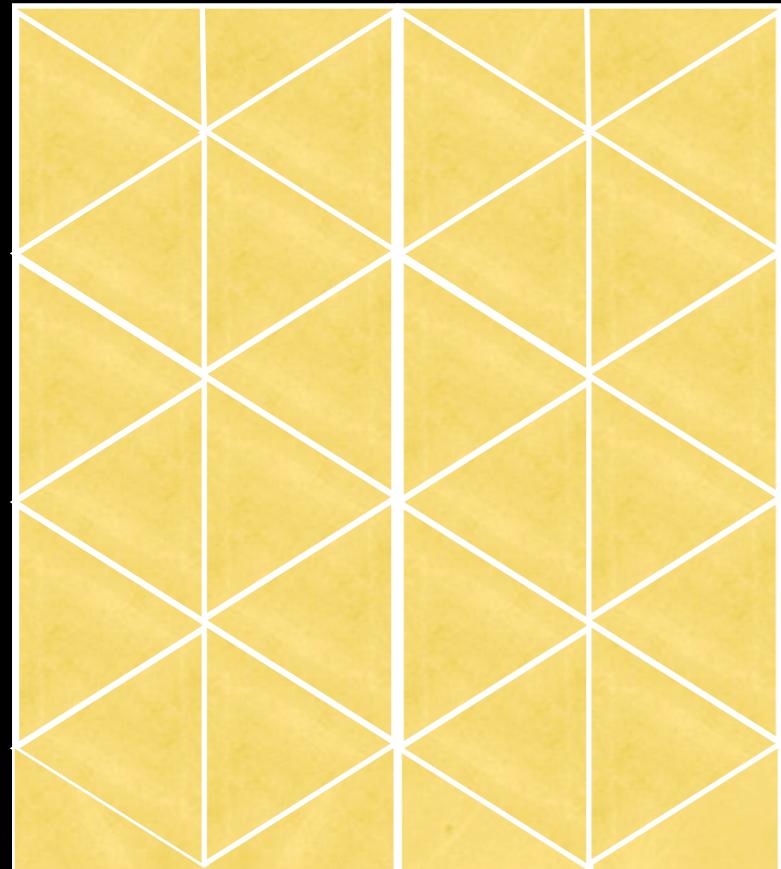
- with high probability, execution time is

$$T_p \leq T_1 / P + O(D)$$

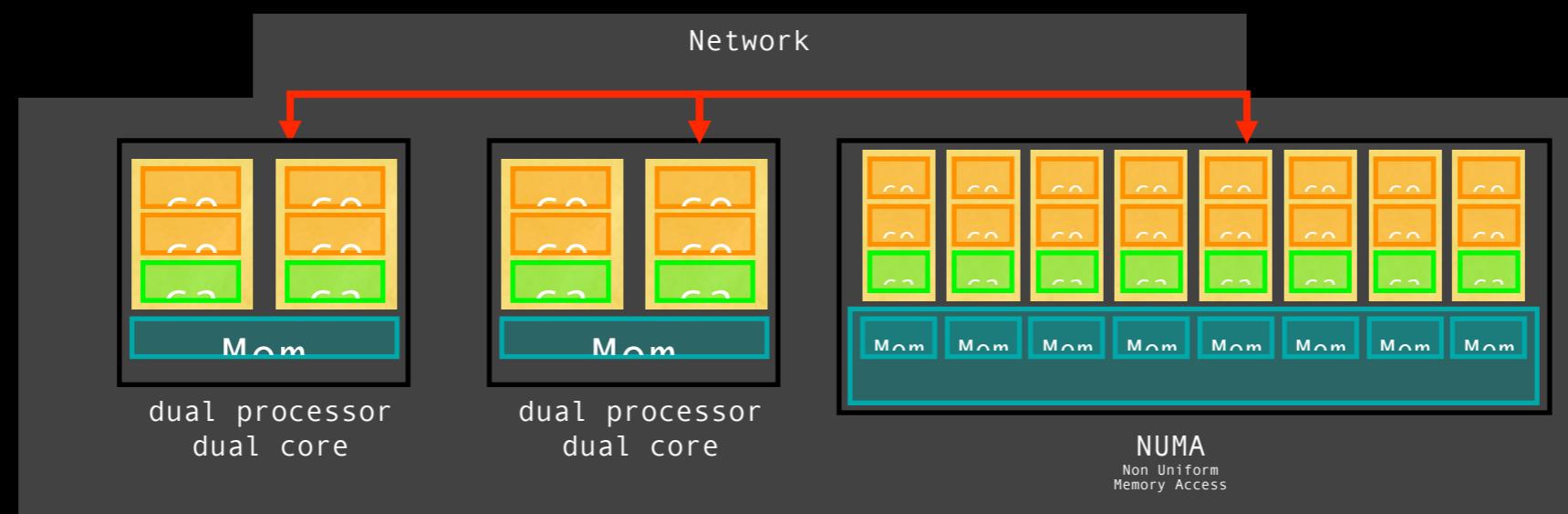
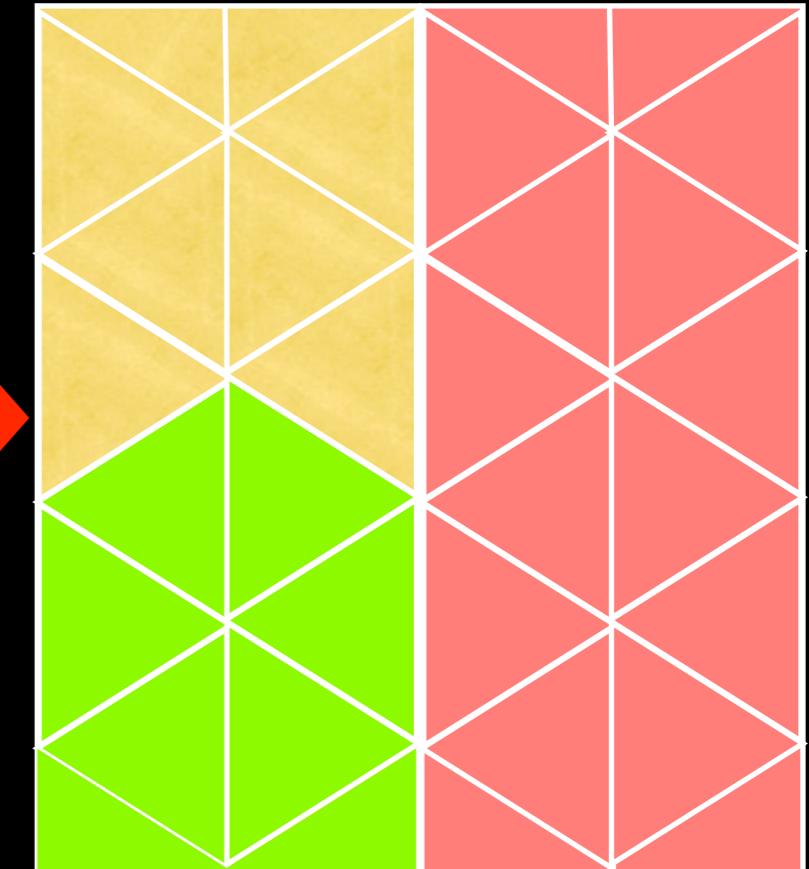
# Domain decomposition



# Domain decomposition



Graph partitioner  
- scotch  
- metis  
- hierarchical :  
ANR DISCOGRID



# That's all ?

- Domain decomposition
  - Data = sub domain, mapped onto machines
  - Task : mapped using “owner compute rule”
- Program : one process per subdomain

```
while (error < epsilon)
{
    exchange interface
    do computation inside subdomain
    compute error
}
```

# That's all ?

- Domain decomposition
  - Data = sub domain, mapped onto machines
  - Task : mapped using “owner compute rule”
- Program : one process per subdomain

```
while (error < epsilon)
{
    exchange interface
    do computation inside subdomain
    compute error
}
```

Communication  
between neighbors



# That's all ?

- Domain decomposition
  - Data = sub domain, mapped onto machines
  - Task : mapped using “owner compute rule”
- Program : one process per subdomain

```
while (error < epsilon)
```

```
{
```

```
    exchange interface
```

```
    do computation inside subdomain
```

```
    compute error
```

```
}
```

Communication  
between neighbors

Global reduction  
communication

# Improvement

- Assume that emission & reception of message are concurrent with local computation

```
while (error < epsilon)
{
    begin send message to my neighbors
    do internal computation
    wait until all messages have been received
    update internal computation
    compute error
}
```

# Improvement

- Assume that emission & reception of message are concurrent with local computation

```
while (error < epsilon)
{
    begin send message to my neighbors
    do internal computation
    wait until all messages have been received
    update internal computation
    compute error
}
```

may overlap  
some delay of  
communication

# How to program

- MPI, standard but low level API
  - scheduling and mapping should be coded
  - bad overlapping of communication by computation (at least in public domain implementation)
  - bad support multi-threaded computations
  - bad support for inter-cluster communication
- Research languages
  - UPC, Titanium, X10, Fortress
  - Our language: Athapascan (API) with Kaapi
  - AUTOMATIC SCHEDULING : <http://moais.imag.fr>

# Experiments

## ● Code

- Kaapi / C++ code versus Fortran MPI code

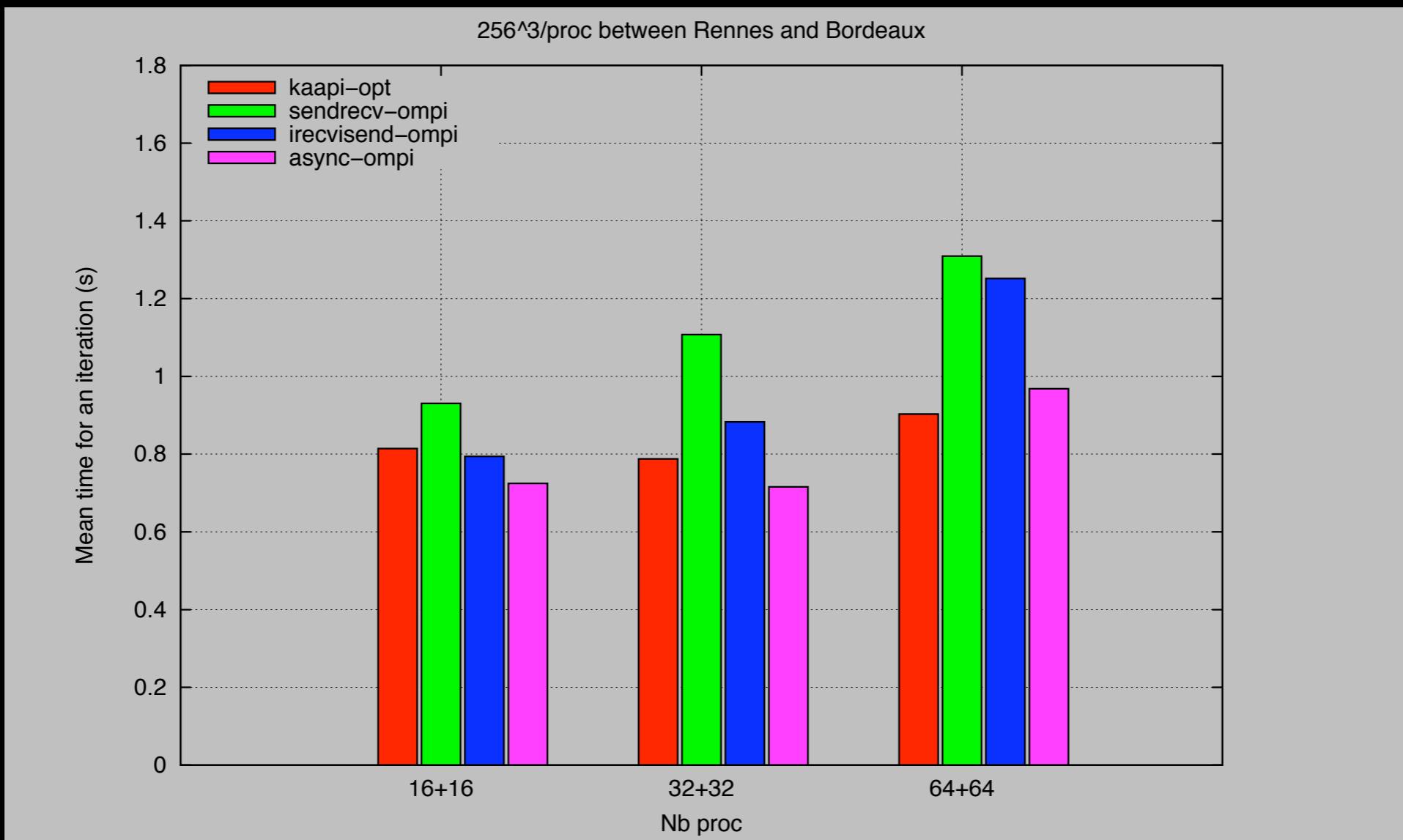
## ● Platform

- Cluster : N processors on a cluster
- Grid : N/4 processors per cluster, 4 clusters

D=256^3	# processors	Cluster (s)	Grid (s)	Overhead
KAAPI	1	0.49	0.49	-
	64	0.55	0.84	0,53
	128	0.65	0.91	0,4
MPI	1	0.44	0.44	-
	64	0.66	2.02	2,06
	128	0.68	1.57	1,31

# Optimized Poisson 3D

- Fortran code with non-blocking IO
  - MPI\_ISend, MPI\_IRecv + MPI\_Wait\_all
  - Overlapping of communication by computation



# Conclusion

## ● SCHEDULING

- but also compilation, grid-reservation, parallel launching, runtime environment, firewall management, ...

## ● More references

- Herlihy, M. and Shavit, N. **The Art of Multiprocessor Programming**, ISBN 0123705916. Morgan Kaufmann Publishing, 2008.
- Foster I., Kesselman C. **The GRID 2: Blueprint for a New Computing Infrastructure**, ISBN 1558609334. Morgan Kauffman Publishing, 2 edition, 1999.
- **Petascale Computing: Algorithms and Applications**, D. Bader (Editor), ISBN 1584889098, Chapman & Hall/CRC, 2007
- **Parallel Algorithms and Cluster Computing: Implementations, Algorithms and Applications**. Karl Heinz Hoffmann (Editor), Arnd Meyer (Editor), ISBN 3540335390, Springer, 2006.

